Software Model Checking

Introduction to Process Algebra

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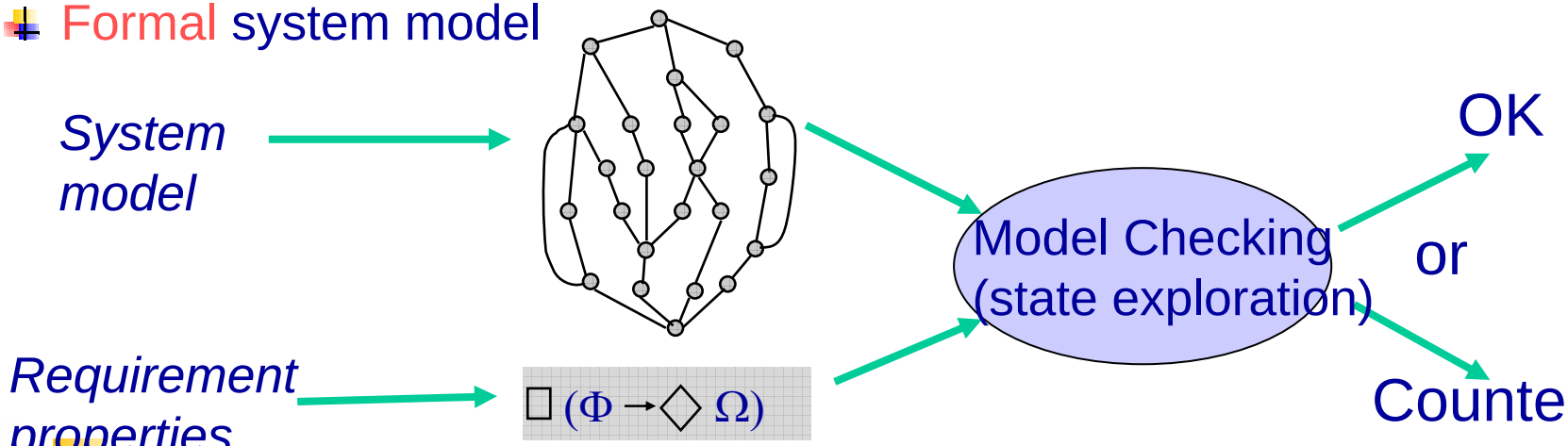
Review of the Previous Class

- We have seen tragic accidents due to software and specification bugs
- These bugs are hard to find because those bugs occurs only in “exceptional” cases
- Informal system specification and requirement specification makes automatic analysis infeasible, which results in incomplete coverage
- To provide better coverage, we need
  - Formal requirement specification
  - Formal system model



Outline

- Requirement specification problems
- Viewpoint on “meaning”(semantics) of system
- Complexity of a system
- Formal modeling v.s. programming
- Introduction to process algebra

Requirement Specification Problems

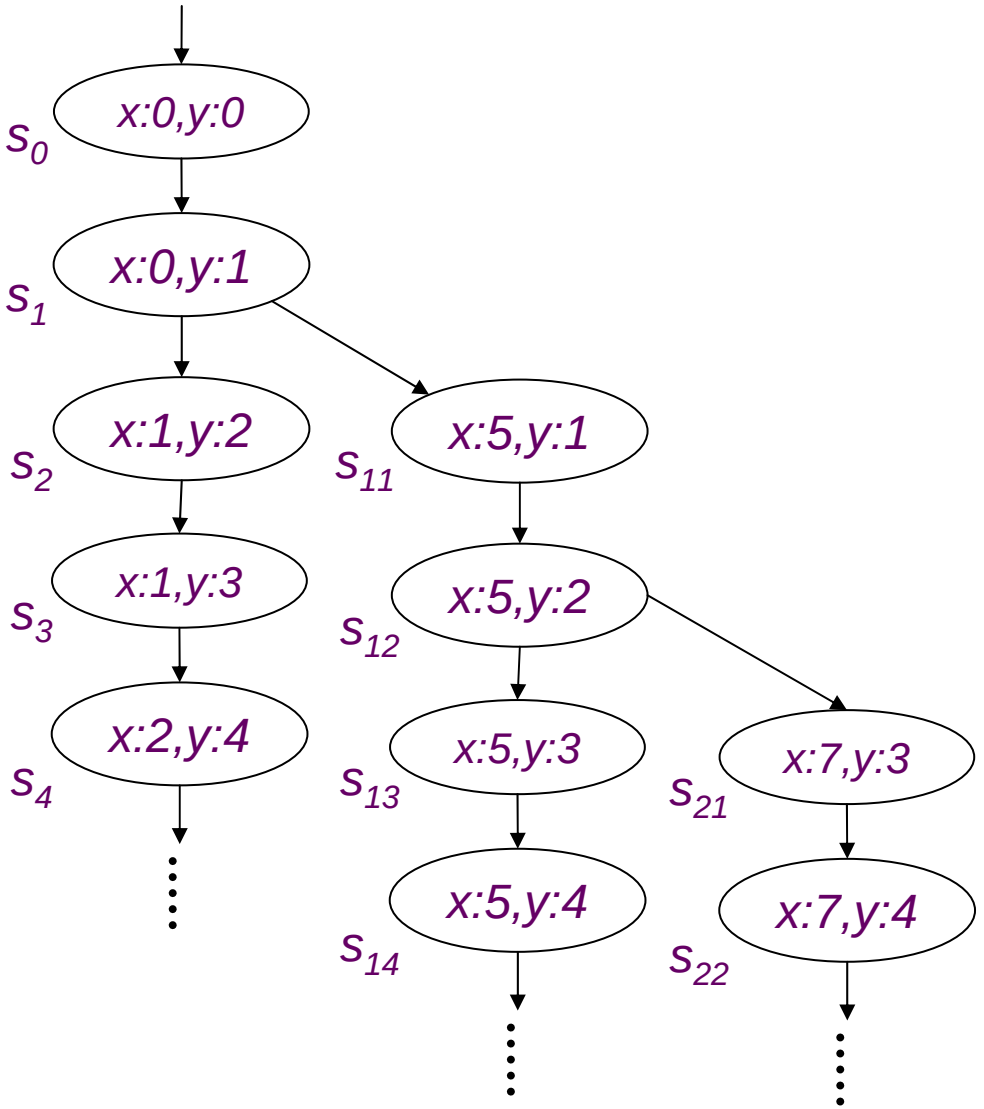
- Ambiguity
  - Expression does not have unique meaning, but can be interpreted as several different meaning.
    - Ex. `int` type in C programming language
- Incompleteness
  - Relevant issues are not addressed , e.g. what to do when user errors occur or software faults show.
    - Ex. See next slides
- Inconsistency
  - Contradictory requirements in different parts of the specification.

Example (retail chain management software)

- If the sales for the current month are below the target sales, then a report is to be printed,
  - unless the difference between target sales and actual sales is less than half of the difference between target sales and actual sales in the previous month
  - or if the difference between target sales and actual sales for the current month is under 5 percent.

Viewpoint on Semantics of a System

- A system execution σ is a sequence of states $s_0 s_1 \ldots$
  - A state has an environment ρ_s:*Var-> Val*
- A system has its semantics as a set of system executions

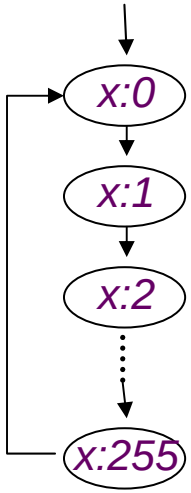


Complexity of Systems

- The complexity of a system is sometimes more accurately expressed using semantic viewpoint (# of reachable states) rather than syntactic viewpoint (line # of source code)
  - the number of different *states* a system can reach
    - Ex> An integer has 2^{32} (~4000000000) possible values

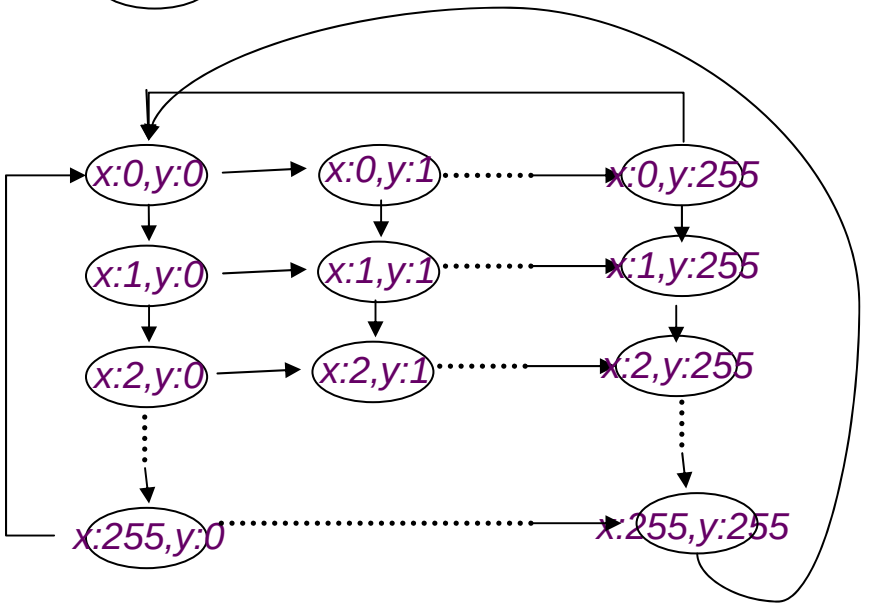
Example

```
active type A() {
byte x;
again:
     x++;
    goto again;
}
```




```
active type A() {
byte x;
again:
     x++;
    goto again;
}

active type B() {
byte y;
again:
     y++;
   goto again;
}
```



Formal Modeling V.S. Programming

		Formal Modeling	Programming
Static Aspects	Abstraction Level	High	Low
	Development Time	Short	Long
Dynamic Aspects	Executable	Yes (model checking) No (theorem proving)	Always
	System Semantics	Mathematically defined	Usually given by examples
	Environment Semantics (i.e. testbeds)	Mathematically defined	Usually given by examples
	Program State Space	Manageable (i.e. tractable state space)	Unmanageable (i.e. beyond computing power)
	Validation	By exhaustive exploration or deductive proof	By testing (incomplete coverage)

Process Algebra

- A process algebra consists of
  - a set of operators and syntactic rules for constructing processes
  - a semantic mapping which assigns meaning or interpretation to every process
  - a notion of equivalence or partial order between processes
- Advantages: A large system can be broken into simpler subsystems and then proved correct in a modular fashion.
  - A hiding or restriction operator allows one to abstract away unnecessary details.
  - Equality for the process algebra is also a congruence relation; and thus, allows the substitution of one component with another equal component in large systems.

Calculus of Communicating Systems (CCS)

- Developed by R.Milner (Univ. of Cambridge)
  - ACM Turing Award 1991
- Provides many interesting paradigms
  - Emphasis on communication and concurrency
    - Provides compact representation on both communication and concurrency
      - Ex> a (receive) and a' (send)
      - Ex> | (parallel operator)
  - Provides observation based abstraction
    - Hiding internal behaviors using \ (restriction) operator, i.e., considering all internal behaviors as an invisible special action τ
  - Provides correctness claim based on equivalence
    - Branching time based equivalence
      - Strong equivalence v.s. weak equivalence

Overview on CCS Syntax and Semantics

- CCS describes a system as a set of communicating Processes
- Behavior of a process is expressed using actions
  - Act =input_actions U output_actions U {τ}
- Each process is built based on the following 7 operators
  - Nil (null-ary opeartor): 0
  - Prefix: a.P
  - Definition: P = a.b.Q
  - Choice: a.P + b.P
  - Parallel: P | Q
  - Restriction: P \ {a,b}
  - Relabelling: P[a/b]
- Each operator has a clear formal semantics via inference rules (premises-conclusion rules)
  - Based on these inference rules, a meaning/semantincs of a process is given as a labelled transition system

Example of a CCS System

- A set of actions Act = {a,a',b,τ}
- We define a CCS system Sys as
  - Sys = (a.E + b.0) | a'.F
- Sys can executes one of the following 4 actions
  - Sys –a-> E | a'F
  - Sys –a'-> (a.E + b.0)|F
  - Sys –b-> 0 | a'.F
  - Sys - τ-> E|F

$$\text{Prefix}\ \frac{}{a.E\ \text{–a->}\ E}$$

$$\text{Choice}_L\ \frac{}{(a.E + b.0)\ \text{–a->}\ E}$$

$$\text{Par}_L\ \frac{}{\mathbf{(a.E + b.0)) \mid a'.F\ \text{–a->}\ E \mid a'.F}}$$